

**Page 1: Question 1 Part 1**

Let  $y = 5 \cos[2(x - \frac{\pi}{6})] - 2$ . Fill in the blanks. Simplify your answers.

Middle  $y$  - value = \_\_\_\_\_

Phase shift = \_\_\_\_\_

Amplitude = \_\_\_\_\_

Period = \_\_\_\_\_

Maximum  $y$  - value = \_\_\_\_\_

Quarter-period = \_\_\_\_\_

Minimum  $y$  - value = \_\_\_\_\_

Find the  $x$  - and  $y$  - coordinates for all points corresponding to the middle, top and bottom of the graph of the function for 2 complete cycles, starting at the phase shift. State clearly if the point corresponds to the top, middle or bottom of the graph.

Point 1:  $x =$  \_\_\_\_\_  $y =$  \_\_\_\_\_ (\_\_\_\_\_)  
 PHASE SHIFT TOP, MIDDLE or BOTTOM

Point 2:  $x =$  \_\_\_\_\_ + \_\_\_\_\_ = \_\_\_\_\_  $y =$  \_\_\_\_\_ (\_\_\_\_\_)  
 PREVIOUS QUARTER- TOP, MIDDLE or  
 $x$  - VALUE PERIOD BOTTOM

Point 3:  $x =$  \_\_\_\_\_ + \_\_\_\_\_ = \_\_\_\_\_  $y =$  \_\_\_\_\_ (\_\_\_\_\_)  
 PREVIOUS QUARTER- TOP, MIDDLE or  
 $x$  - VALUE PERIOD BOTTOM

Point 4:  $x =$  \_\_\_\_\_ + \_\_\_\_\_ = \_\_\_\_\_  $y =$  \_\_\_\_\_ (\_\_\_\_\_)  
 PREVIOUS QUARTER- TOP, MIDDLE or  
 $x$  - VALUE PERIOD BOTTOM

Point 5:  $x =$  \_\_\_\_\_ + \_\_\_\_\_ = \_\_\_\_\_  $y =$  \_\_\_\_\_ (\_\_\_\_\_)  
 PREVIOUS QUARTER- TOP, MIDDLE or  
 $x$  - VALUE PERIOD BOTTOM

Point 6:  $x =$  \_\_\_\_\_ + \_\_\_\_\_ = \_\_\_\_\_  $y =$  \_\_\_\_\_ (\_\_\_\_\_)  
 PREVIOUS QUARTER- TOP, MIDDLE or  
 $x$  - VALUE PERIOD BOTTOM

Point 7:  $x =$  \_\_\_\_\_ + \_\_\_\_\_ = \_\_\_\_\_  $y =$  \_\_\_\_\_ (\_\_\_\_\_)  
 PREVIOUS QUARTER- TOP, MIDDLE or  
 $x$  - VALUE PERIOD BOTTOM

Point 8:  $x =$  \_\_\_\_\_ + \_\_\_\_\_ = \_\_\_\_\_  $y =$  \_\_\_\_\_ (\_\_\_\_\_)  
 PREVIOUS QUARTER- TOP, MIDDLE or  
 $x$  - VALUE PERIOD BOTTOM

Point 9:  $x =$  \_\_\_\_\_ + \_\_\_\_\_ = \_\_\_\_\_  $y =$  \_\_\_\_\_ (\_\_\_\_\_)  
 PREVIOUS QUARTER- TOP, MIDDLE or  
 $x$  - VALUE PERIOD BOTTOM

**Page 2: Question 2 Part 1**

Let  $y = -3\sin(\frac{3\pi}{2}x + \frac{9\pi}{8}) + 4$ . Fill in the blanks. Simplify your answers.

Middle  $y$  - value = \_\_\_\_\_

Phase shift = \_\_\_\_\_

Amplitude = \_\_\_\_\_

Period = \_\_\_\_\_

Maximum  $y$  - value = \_\_\_\_\_

Quarter-period = \_\_\_\_\_

Minimum  $y$  - value = \_\_\_\_\_

Find the  $x$  - and  $y$  - coordinates for all points corresponding to the middle, top and bottom of the graph of the function for 2 complete cycles, starting at the phase shift. State clearly if the point corresponds to the top, middle or bottom of the graph.

Point 1:  $x =$  \_\_\_\_\_  $y =$  \_\_\_\_\_ (\_\_\_\_\_)  
 PHASE SHIFT TOP, MIDDLE or BOTTOM

Point 2:  $x =$  \_\_\_\_\_ + \_\_\_\_\_ = \_\_\_\_\_  $y =$  \_\_\_\_\_ (\_\_\_\_\_)  
 PREVIOUS QUARTER- TOP, MIDDLE or  
 $x$  - VALUE PERIOD BOTTOM

Point 3:  $x =$  \_\_\_\_\_ + \_\_\_\_\_ = \_\_\_\_\_  $y =$  \_\_\_\_\_ (\_\_\_\_\_)  
 PREVIOUS QUARTER- TOP, MIDDLE or  
 $x$  - VALUE PERIOD BOTTOM

Point 4:  $x =$  \_\_\_\_\_ + \_\_\_\_\_ = \_\_\_\_\_  $y =$  \_\_\_\_\_ (\_\_\_\_\_)  
 PREVIOUS QUARTER- TOP, MIDDLE or  
 $x$  - VALUE PERIOD BOTTOM

Point 5:  $x =$  \_\_\_\_\_ + \_\_\_\_\_ = \_\_\_\_\_  $y =$  \_\_\_\_\_ (\_\_\_\_\_)  
 PREVIOUS QUARTER- TOP, MIDDLE or  
 $x$  - VALUE PERIOD BOTTOM

Point 6:  $x =$  \_\_\_\_\_ + \_\_\_\_\_ = \_\_\_\_\_  $y =$  \_\_\_\_\_ (\_\_\_\_\_)  
 PREVIOUS QUARTER- TOP, MIDDLE or  
 $x$  - VALUE PERIOD BOTTOM

Point 7:  $x =$  \_\_\_\_\_ + \_\_\_\_\_ = \_\_\_\_\_  $y =$  \_\_\_\_\_ (\_\_\_\_\_)  
 PREVIOUS QUARTER- TOP, MIDDLE or  
 $x$  - VALUE PERIOD BOTTOM

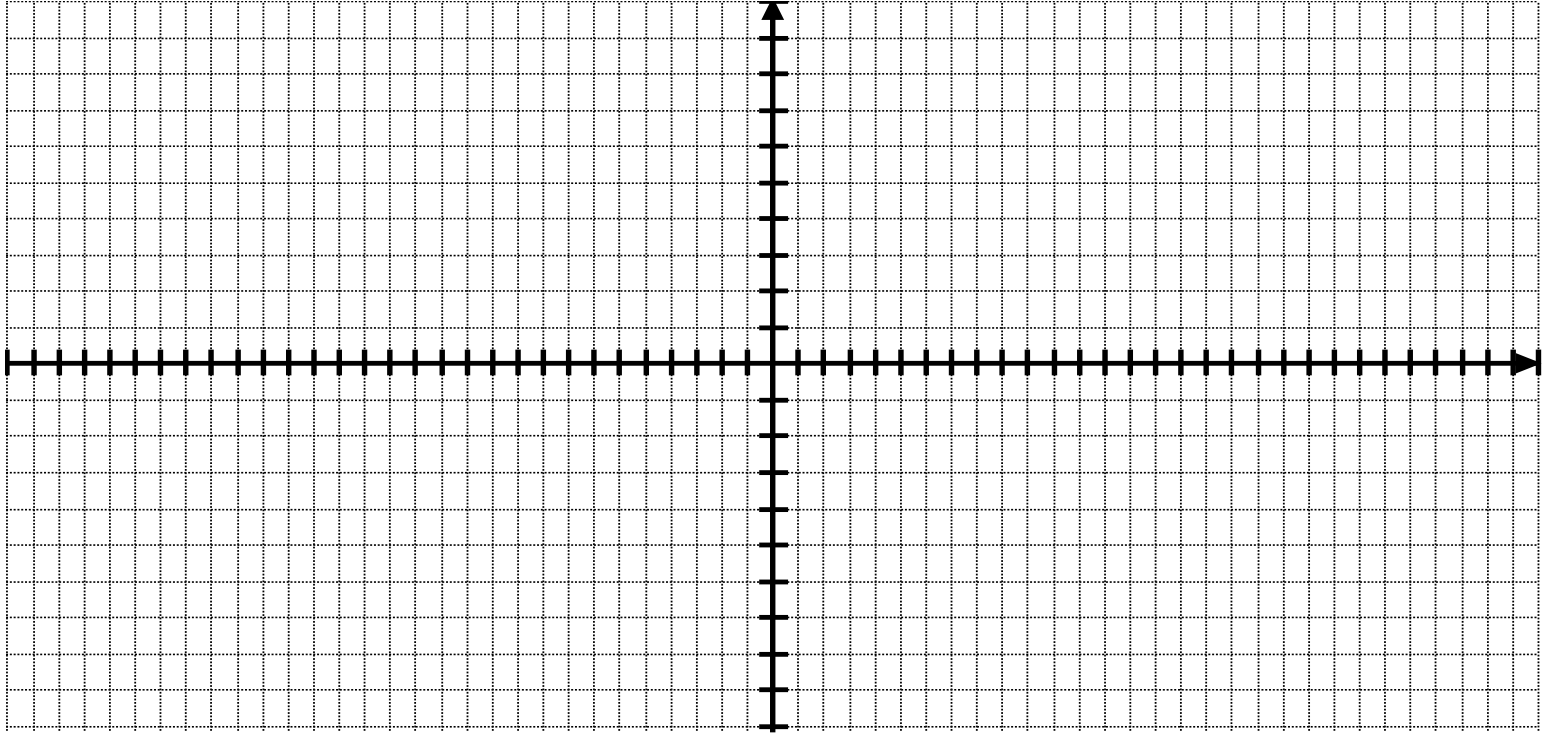
Point 8:  $x =$  \_\_\_\_\_ + \_\_\_\_\_ = \_\_\_\_\_  $y =$  \_\_\_\_\_ (\_\_\_\_\_)  
 PREVIOUS QUARTER- TOP, MIDDLE or  
 $x$  - VALUE PERIOD BOTTOM

Point 9:  $x =$  \_\_\_\_\_ + \_\_\_\_\_ = \_\_\_\_\_  $y =$  \_\_\_\_\_ (\_\_\_\_\_)  
 PREVIOUS QUARTER- TOP, MIDDLE or  
 $x$  - VALUE PERIOD BOTTOM

Sketch a detailed graph of 2 complete cycles of  $y = 5 \cos[2(x - \frac{\pi}{6})] - 2$  using the information from Question 1 Part 1.

You must label all  $x$  - and  $y$  - values from Part 1 on the appropriate axes below, and you must use a consistent scale for each axis.

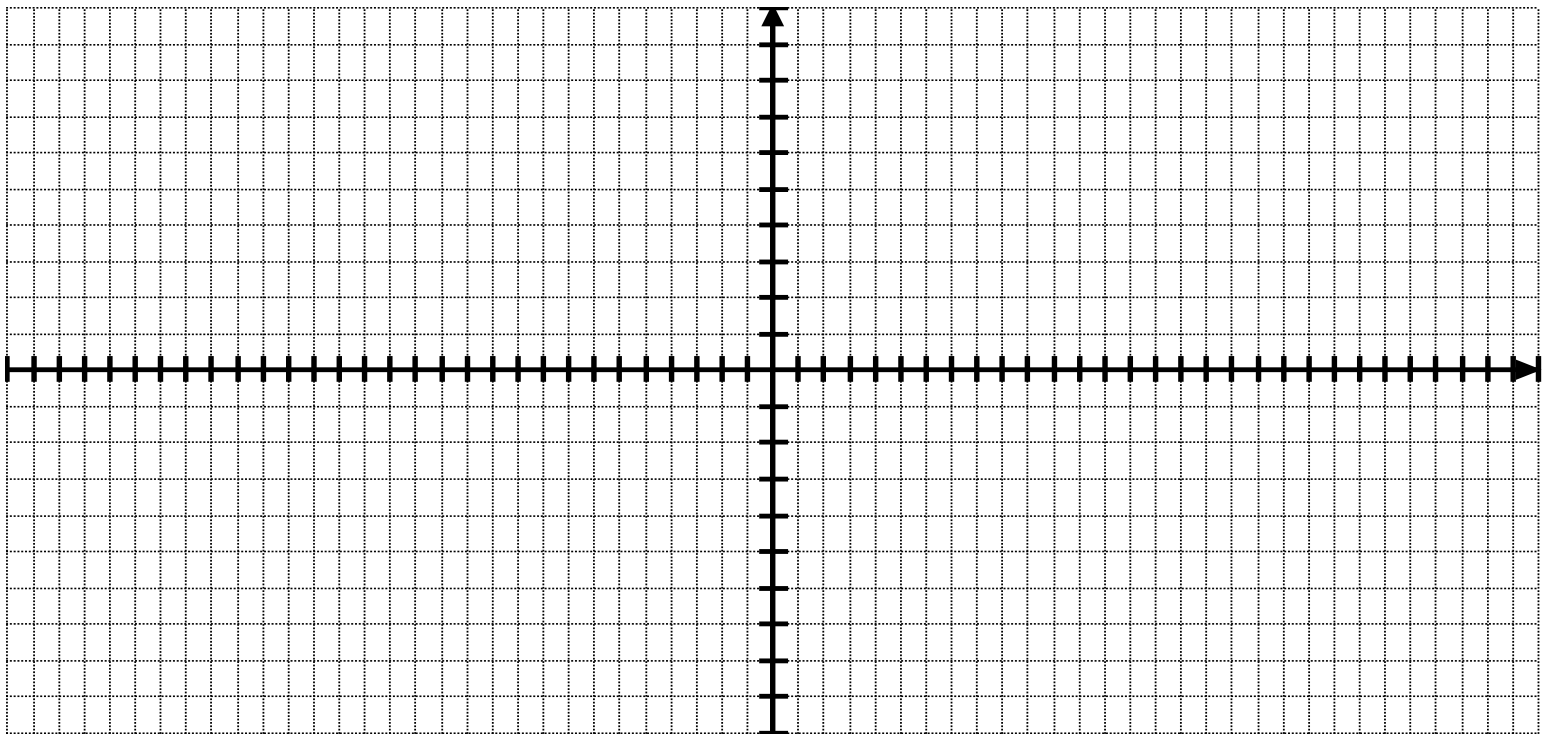
**You do NOT need to label each tick mark on each axis, only the ones you found in Part 1.**



Sketch a detailed graph of 2 complete cycles of  $y = -3 \sin(\frac{3\pi}{2}x + \frac{9\pi}{8}) + 4$  using the information from Question 2 Part 1.

You must label all  $x$  - and  $y$  - values from Part 1 on the appropriate axes below, and you must use a consistent scale for each axis.

**You do NOT need to label each tick mark on each axis, only the ones you found in Part 1.**



**Page 4: Question 3**

Fill in the blanks regarding the graph on the right (which is NOT drawn to scale). Simplify your answers.

NOTE: The  $x$  – coordinates of the two points highlighted are  $-\frac{\pi}{9}$  and  $\frac{11\pi}{9}$ ,  
and correspond to points with the middle  $y$  – value.

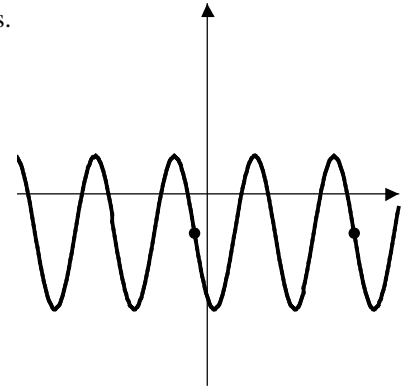
The maximum and minimum  $y$  – values are 2 and  $-5$ .

Middle  $y$  – value = \_\_\_\_\_ =  $D$

Amplitude = \_\_\_\_\_ =  $|A|$

Phase shift = \_\_\_\_\_ =  $C$

Period = \_\_\_\_\_ =  $\frac{2\pi}{B} \Rightarrow B =$  \_\_\_\_\_



Given the points shown, the equation of the graph is easier to write using a \_\_\_\_\_ function,  
 POSITIVE or NEGATIVE      SIN or COS

So,  $A =$  \_\_\_\_\_.

The equation of the graph is  $y =$  \_\_\_\_\_  $(x -$  \_\_\_\_\_  $) +$  \_\_\_\_\_.  
 A      SIN or COS      B      C      D

You are riding a ferris wheel with a radius of 84 feet, which is turning at a regular rate.

You have a tremendous fear of heights, but you don't want to embarrass yourself in front of your date, so you try to distract yourself by finding an equation for your height ( $y$ ) as a function of time ( $t$ ).

At time  $t = 12$  seconds, you are at the bottom of the wheel, which is 4 feet above the ground.

At time  $t = 27$  seconds, you are at the top of the wheel. (This is the first time you reach the top after time  $t = 12$  seconds.)

Fill in the blanks. Simplify your answers.

It may be helpful to draw a crude sketch of the height function and label the known  $t$  – and  $y$  – values on it.

Maximum  $y$  – value = \_\_\_\_\_      Phase shift = \_\_\_\_\_ =  $C$

Minimum  $y$  – value = \_\_\_\_\_      Period = \_\_\_\_\_ =  $\frac{2\pi}{B}$

Middle  $y$  – value = \_\_\_\_\_ =  $D$        $B =$  \_\_\_\_\_

Amplitude = \_\_\_\_\_ =  $|A|$

Given the crude sketch of the height function, the equation is easier to write using a \_\_\_\_\_ function,  
 POSITIVE or NEGATIVE      SIN or COS

So,  $A =$  \_\_\_\_\_.

The equation of the function is  $y =$  \_\_\_\_\_  $(t -$  \_\_\_\_\_  $) +$  \_\_\_\_\_.  
 A      SIN or COS      B      C      D